Divide-and-conquer

- Each *task* recursively creates n tasks that divide the problem into subproblems
- Each task t then waits for all n tasks to finish and then may 'combine' the responses
- At some point the recursion stops (at the bottom of the tree), and some sequential kernel is executed
- Then the result is propagated upward in the tree recursively
- Examples: fibonacci, quick sort, ...

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State-space search

- Each *task* recursively creates *n* tasks to partition the search space
- If the problem is one-solution search, as soon as a task encounters a solution, the program may need to terminate
 - ★ Kill-chasing problem
- All-solution search may require behaviour much like divide-and-conquer where values are combined
 - Example: all-solution nqueens
 - Number of solutions are accumulated recursively up the tree

- Each Fib chare is a task that performs one of two actions:
 - Creates two new Fib chares to compute fib(n-1) and fib(n-2) and then waits for the response, adding up the two responses when they arrive
 - ★ After both arrive, sends a response message with the result to the parent task
 - * Or prints the value and calls CkExit() if it is the root
 - ► If n = 1 or n = 0 (passed down from the parent) it sends a response message with n back to the parent task

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```
mainmodule fib {
    mainchare Main {
        entry Main(CkArgMsg* m);
    };
    chare Fib {
        entry Fib(int n, bool isRoot, CProxy_Fib parent);
        entry void response(int value);
    };
};
```

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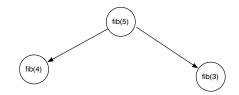
Fibonacci Example

```
struct Main : public CBase_Main {
  Main(CkArgMsg* m) {
    CProxy_Fib::ckNew(atoi(m->argv[1]), true, CProxy_Fib());
};
struct Fib : public CBase_Fib {
  CProxy_Fib parent; bool isRoot; int result, count;
  Fib(int n, bool isRoot_, CProxy_Fib parent_)
    : parent(parent_), isRoot(isRoot_), result(0), count(n < 2? 1 : 2) {
    if (n < 2) response(n);
    else {
      CProxy_Fib::ckNew(n - 1, false, thisProxy);
      CProxy_Fib::ckNew(n - 2, false, thisProxy);
  void response(int val) {
    result += val;
    if (--\text{count} == 0) {
      if (isRoot) {
        CkPrintf("Fibonacci number is: %d\n", result);
        CkExit();
      } else {
        parent.response(result);
        delete this;
```

(fib(5)

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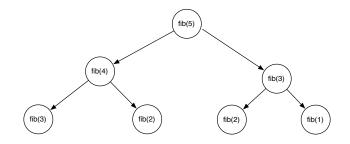
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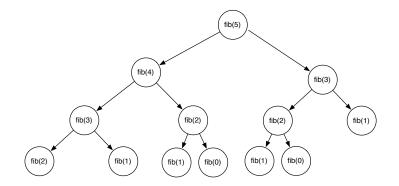
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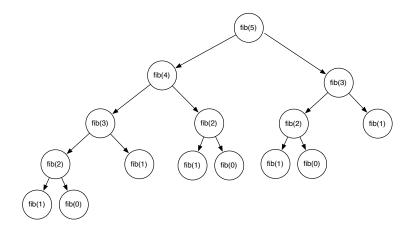
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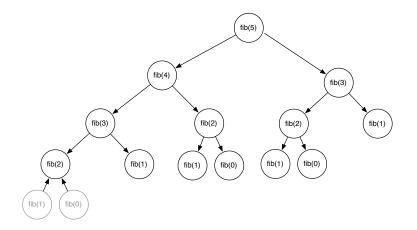


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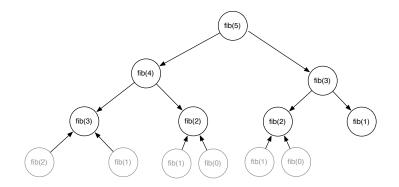


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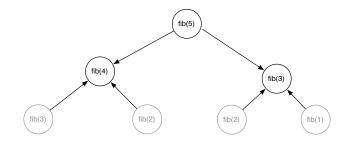


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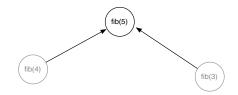


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(fib(5)

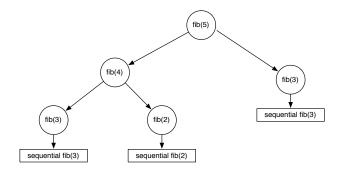
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- How much work/computation does each chare do in this example?
- What are some of the overheads of this approach?
- Is there way we can reduce/amortize the overhead?

Possible Solution

- Set a sequential threshold in the computational tree
 - Past this threshold (i.e. when n < threshold), instead of constructing two new chares, compute the fibonacci sequentially



fib(5), fib(4) are fine grains, fib(3), fib(2) are coarser grains
The coarser grains now amortize the cost of the fine-grained execution

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Fibonacci w/Threshold Example

```
#define THRESHOLD 10
struct Main : public CBase_Main { /* ... same as before ... */ };
struct Fib : public CBase_Fib {
  CProxy_Fib parent: bool isRoot: int result, count:
  Fib(int n, bool isRoot_, CProxy_Fib parent_)
    : parent(parent_), isRoot(isRoot_), result(0), count(n < THRESHOLD ? 1 : 2) {
    if (n < THRESHOLD) response(seqFib(n));
    else {
      CProxy_Fib::ckNew(n - 1, false, thisProxy):
      CProxy_Fib::ckNew(n - 2, false, thisProxy);
  int seqFib(int n) { return (n < 2) ? n : seqFib(n - 1) + seqFib(n - 2); }
  void response(int val) {
    result += val;
    if (--count == 0) {
      if (isRoot) {
        CkPrintf("Fibonacci number is: %d\n", result);
        CkExit();
      } else {
        parent.response(result);
        delete this;
```

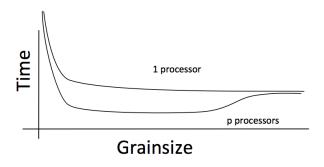
Amdahlss Law and Grainsize

- Original "law":
 - If a program has K% sequential section, then speedup is limited to $\frac{100}{K}$.
 - ★ If the rest of the program is parallelized completely
- Grainsize corollary:
 - ▶ If any individual piece of work is > K time units, and the sequential program takes T_{seq},
 - **★** Speedup is limited to $\frac{T_{seq}}{K}$
- So:
 - Examine performance data via histograms to find the sizes of remappable work units
 - If some are too big, change the decomposition method to make smaller units

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Grainsize

• (working) Definition: the amount of computation per potentially parallel event (task creation, enqueue/dequeue, messaging, locking. .)

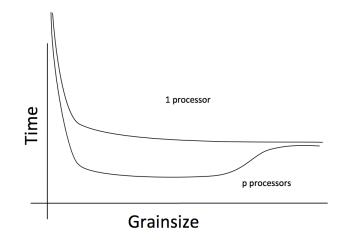


Grainsize and Overhead

- What is the ideal grainsize?
- Should it depend on the number of processors?

$$T_{1} = T\left(1 + \frac{v}{g}\right)$$
$$T_{p} = max\left\{g, \frac{T_{1}}{p}\right\}$$
$$T_{p} = max\left\{g, \frac{T\left(1 + \frac{v}{g}\right)}{p}\right\}$$
$$v: \text{ overhead per message,}$$
$$T_{p}: p \text{ processor completion time}$$
$$g: \text{ grainsize (computation per message)}$$

Grainsize and Scalability



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- Make it as small as possible, as long as it amortizes the overhead
- More specifically, ensure:
 - Average grainsize is greater than kv (say 10v)
 - No single grain should be allowed to be too large
 - ***** Must be smaller than $\frac{T}{n}$, but actually we can express it as:
 - * Must be smaller than kmv (say 100v)
- Important corollary:
 - You can be at close to optimal grainsize without having to think about p, the number of processors

How to determine/ensure grainsize

- Compiler techniques can help, but only in some cases
 - Note that they don't need precise determination of grainsize, just one that will satisfy a broad inequality
 - ★ kv < g < mkv (10v < g < 100v)

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